15.12 First we balance the equation:

$$PCl_{5}(g) + 4 H_{2}O(l) \longrightarrow 5 HCl(aq) + H_{3}PO_{4}(aq)$$

$$\Delta G^{\circ}_{r} = 5(-131.23 \text{ kJ} \cdot \text{mol}^{-1}) + (-1142.54 \text{ kJ} \cdot \text{mol}^{-1})$$

$$- [(-305.0 \text{ kJ} \cdot \text{mol}^{-1}) + 4(-237.13 \text{ kJ} \cdot \text{mol}^{-1})]$$

$$= -545.17 \text{ kJ} \cdot \text{mol}^{-1}$$

The reaction is spontaneous.

15.42 Because there is no data available for the free energy of formation of HClO, we must turn to the electrochemical data in Appendix 2B. The appropriate half-reactions are

$$Cl_2 + 2 e^- \longrightarrow 2 Cl^ E^\circ = +1.36 \text{ V}$$

$$\frac{Cl_2 + 2 \text{ H}_2\text{O} \longrightarrow 2 \text{ HClO} + 2 \text{ H}^+ + 2 e^-}{2 \text{ Cl}_2 + 2 \text{ H}_2\text{O} \longrightarrow 2 \text{ HClO} + 2 \text{ H}^+ + 2 \text{ Cl}^-}$$
  $E^\circ = -0.27 \text{ V}$ 

The  $E^{\circ}$  will be the same for the reaction balanced as

$$Cl_2 + H_2O \longrightarrow HCIO + H^+ + CI^ E^\circ = -0.27 \text{ V}$$

but n will be  $1 e^-$  rather than  $2 e^-$  as in the previous equation.

 $\Delta G^{\circ}_{r}$  can now be calculated from  $\Delta G^{\circ}_{r} = -nFE^{\circ}$ 

$$\Delta G_r^{\circ} = -(1)(96 \ 485 \ \text{J} \cdot \text{V}^{-1} \cdot \text{mol}^{-1})(-0.27 \ \text{V}) = +26 \ \text{kJ} \cdot \text{mol}^{-1}$$

(b) The equilibrium constant can be calculated from  $\Delta G^{\circ}_{r} = -RT \ln K$ 

$$K = e^{\frac{\Delta G_{\rm r}^{\circ}}{RT}} = e^{\frac{26\ 000\ \text{J}\cdot\text{mol}^{-1}}{(8.314\ \text{J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1})(298\ \text{K})}} \cong 2.8 \times 10^{-5}$$

15.84 The balanced chemical equation is:

$$2 \text{ K}_2 \text{MnF}_6 + 4 \text{ SbF}_5 \rightarrow 4 \text{ KSbF}_6 + 2 \text{ MnF}_3 + \text{F}_2$$

The amount, in moles, of F<sub>2</sub> produced is found by:

$$\frac{125 \text{ g K}_2 \text{MnF}_6}{247.14 \text{ g} \cdot \text{mol}^{-1}} \left( \frac{1 \text{ mol } \text{F}_2}{2 \text{ mol } \text{K}_2 \text{MnF}_6} \right) = 0.253 \text{ mol } \text{F}_2$$

The volume of this amount of fluorine gas is:

$$V = \frac{nRT}{P} = \frac{(0.253 \text{ mol})(0.08206 \text{ L} \cdot \text{atm} \cdot \text{K}^{-1} \cdot \text{mol}^{-1})(298 \text{ K})}{1 \text{ atm}}$$
  
= 6.18 L