Chem. 6C Midterm 2  
Version B  
November 13, 2007

Name__________________________________________  
Student Number _________________________________  
TA Name_______________________________________  
Section Time____________________________________

All work must be shown on the exam for partial credit. Points will be taken off for incorrect or no units. Non graphing calculators and two hand-written 3” × 5” note cards are permitted.

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1) Use the following reaction diagram to answer the following questions

(3 pts) Which number represents a reaction intermediate?

2

(3 pts) Which number represents a transition state or an activated complex?

3

(3 pts) Is this reaction endothermic or exothermic?

Exothermic

(5 pts) If an overall reaction has a $\Delta G_{\text{rxn}} = 45 \text{ kJ}$-$\text{mol}^{-1}$ and an activation barrier of $75 \text{ kJ}$-$\text{mol}^{-1}$ what is the activation barrier of the reverse reaction?

30 kJ-$\text{mol}^{-1}$

(6 pts) Draw a reaction diagram for a system without a catalyst and with a catalyst. Make sure to label the diagram (original pathway, catalyzed path way, activation energies, coordinates, reactants and products).
2) (10 pts) The decomposition of hydrogen iodide (2HI(g) → H₂(g) + I₂(g)) has a rate constant of 9.51×10⁻⁹ L·mol⁻¹·s⁻¹ at 500 K and 1.10×10⁻⁵ L·mol⁻¹·s⁻¹ at 600 K. Find Ea? 

\[
\ln(k) = \ln(A) - E_a R^{-1} T^{-1}
\]

Eq1: \(\ln(9.51 \times 10^{-9} \text{ L·mol}^{-1} \cdot \text{s}^{-1}) = \ln(A) - E_a (8.3145 \text{ J·mol}^{-1} \cdot \text{K}^{-1})^{-1} (500 \text{ K}^{-1})\) 
-18.47 = \ln(A) - 2.41×10⁻⁴ \text{ mol·J}^{-1}·E_a

Eq2: \(\ln(1.10 \times 10^{-5} \text{ L·mol}^{-1} \cdot \text{s}^{-1}) = \ln(A) - E_a (8.3145 \text{ J·mol}^{-1} \cdot \text{K}^{-1})^{-1} (600 \text{ K}^{-1})\) 
-11.42 = \ln(A) - 2.00×10⁻⁴ \text{ mol·J}^{-1}·E_a

Eq1 - Eq2 = -18.47 + 11.42 
= \ln(A) - 2.41×10⁻⁴ \text{ mol·J}^{-1}·E_a - \ln(A) + 2.00×10⁻⁴ \text{ mol·J}^{-1}·E_a

-7.05 = -4.10×10⁻⁵ \text{ mol·J}^{-1}·E_a

\[E_a = 1.72 \times 10^5 \text{ J·mol}^{-1}\]

3) (10 pts) A living tree contains \(^{14}\)C (\(t_{1/2} = 5600 \text{ y}\)) and has a specific activity of 750 counts per hour. A wooden artifact of the same size recovered from an archeological site gives a count of 90 counts per hour. What is the age of the artifact?

\[k = \ln 2 / t_{1/2} = \ln 2 / 5600 = 1.24 \times 10^{-4} \text{ y}^{-1}\]

\[\left[A\right]_t = \left[A\right]_0 e^{kt}\]

\[90 = 750 e^{(1.24 \times 10^{-4} \text{ y}^{-1} \cdot t)}\]

\[t = 17089 \text{ y}\]

(6 pts) Explain why carbon dating works?

Carbon-14 enters living things through photosynthesis and digestion of \(^{14}\)CO₂ and leaves organism’s through respiration and excretions. But the ratio of Carbon-12 to Carbon-14 remains constant in living things. When an organism dies it can no longer exchange carbon with its surroundings. The Carbon-14 will slowly decay into Carbon-12 over time. The ratio of Carbon-14 to Carbon-12 can be used to estimate the time since the organism died.
4) The reaction CHCl₃(g) + Cl₂(g) → CCl₄(g) + HCl(g), has been proposed to occur by the following mechanism

Elementary Reactions
(1) Cl₂ ⇌ Cl + Cl  Rapid equilibrium, rate constants k₁ and k₁'
(2) CHCl₃ + Cl → HCl + CCl₃ Slow, rate constant k₂
(3) CCl₃ + Cl → CCl₄ Very Rapid, rate constant k₃

(3 pts) What is the molecularity of each of the elementary reactions?

1  unimolecular
2  bimolecular
3  bimolecular

(5 pts) What assumption is made in the steady state approximation?

The steady state approximation assumes that the concentration of intermediates is constant.

(5 pts) When can the pre-equilibrium condition be used?

The pre-equilibrium condition can be used when intermediates are formed in a rapid equilibrium reaction prior to a slow step in the mechanism.

(8 pts) What is the rate law for this reaction?

Rate = k₂[CHCl₃][Cl]
Pre equilibrium condition
k₁[Cl₂] = k₁'[Cl]² therefore [Cl] = k₁⁻¹/₂k₁'[Cl₂]⁻¹/₂
Rate = k₂·k₁⁻¹/₂·k₁'[Cl₂]⁻¹/₂[CHCl₃]

(5 pts) If the rate law was experimentally found to be k[Cl₂]⁻¹/₂[CHCl₃] then is the given mechanism definitely the mechanism? Explain.

The experimentally found rate law and the rate law derived from the mechanism are the same. Therefore it is possible that the given mechanism is correct. However you can never guarantee that the mechanism is correct because other mechanism can give the same rate law.
5) (3 pts) Nuclides with too many neutrons to be in the band of stability are most likely to decay by what mode?

Beta Particle Emission

(3 pts) The nuclide $^{208}_{81}$Tl is the daughter nuclide resulting from the $\alpha$-decay of what parent nuclide?

$^{212}_{83}$Bi

(4 pts) Which type of particle $\alpha$, $\beta$, or $\gamma$ can penetrate into a surface the farthest and which will do the most damage?

$\gamma$ particles can penetrate the surface the farthest but $\alpha$ particles do the most damage

(3 pts) Electron capture transforms $^{40}_{19}$K into what nuclide?

$^{40}_{18}$Ar

(3 pts) What is the daughter nuclide that is produced when $^{243}_{95}$Am undergoes $\gamma$ emission?

$^{243}_{95}$Am

(6 pts) Calculate the frequency and wavelength of the $\gamma$ radiation emitted as a result of a rearrangement of nucleons in a single daughter nucleus through which $2.2 \times 10^{-14}$ J of energy is released?

\[
E = h \cdot \nu \\
2.2 \times 10^{-14} \text{ J} = (6.626 \times 10^{-34} \text{ J} \cdot \text{s}) \nu \\
\nu = 3.32 \times 10^{19} \text{ Hz} \\
\lambda = \frac{c}{\nu} \\
\lambda = (3.0 \times 10^8 \text{ m/s})(3.32 \times 10^{19} \text{ Hz})^{-1} \\
\lambda = 9.04 \times 10^{-12} \text{ m}
\]
6) (15 pts) A small portion of a cancer patient’s brain is exposed for 27.0 min to 475 Bq of $^{60}$Co for treatment of a tumor. If the brain mass exposed is 1.488 g and each $\beta$ particle emitted has an energy of $5.05 \times 10^{-14}$ J, what is the dose in rads?

\[
t = 27.0 \text{ m} = (27.0 \text{ m})(60 \text{ s} / \text{ m}) = 1620 \text{ s}
\]
Bq is 1 disintegrations per second

Therefore

\[
475 \text{ Bq} = (\text{# of disintegrations}) / (1620 \text{ s})
\]

# of disintegrations = 769500

Each disintegration gives off $5.05 \times 10^{-14}$ J of energy

Therefore the total energy given off is:

\[
\text{# of disintegrations} \times \text{energy each disintegration gives off} = 769500(5.05 \times 10^{-14} \text{ J}) = 3.895 \times 10^{-8} \text{ J}
\]

This radiation is dispersed over a 1.488 g = .001488 kg sample

Therefore the energy / kg = $3.895 \times 10^{-8}$ J / .001488 kg = $2.617 \times 10^{-5}$ J·kg$^{-1}$

1 rad = $10^{-2}$ J·kg$^{-1}$ change units to rads

$2.617 \times 10^{-5}$ J·kg$^{-1}$ (1 rad / $10^{-2}$ J·kg$^{-1}$) = $2.62 \times 10^{-3}$ rad
7) (15 pts) The reaction $2\text{NO}(g) + \text{H}_2(g) \rightarrow \text{N}_2\text{O}(g) + \text{H}_2\text{O}$ has been proposed to happen via the following mechanism

\begin{align*}
\text{NO}(g) + \text{NO}(g) &\rightarrow \text{N}_2\text{O}_2(g) \quad \text{(rate constants $k_1$ and $k_1'$)} \\
\text{N}_2\text{O}_2(g) + \text{H}_2(g) &\rightarrow \text{N}_2\text{O}(g) + \text{H}_2\text{O(l)} \quad \text{(rate constant $k_2$)}
\end{align*}

However nothing is known about the size of the rate constants. Derive an expression for the rate of formation of $\text{N}_2\text{O}$.

Rate of formation of $\text{N}_2\text{O} = k_2[\text{N}_2\text{O}_2][\text{H}_2]$

$\text{N}_2\text{O}_2$ is an intermediate therefore it needs to be eliminated from the rate expression by using the steady state approximation

Rate of formation of $\text{N}_2\text{O}_2 = k_1[\text{NO}]^2$

Rate of consumption of $\text{N}_2\text{O}_2 = k_1'[\text{N}_2\text{O}_2]$

Rate of consumption of $\text{N}_2\text{O}_2 = k_2[\text{N}_2\text{O}_2][\text{H}_2]$

Net rate of formation of $\text{N}_2\text{O}_2 = k_1[\text{NO}]^2 - k_1'[\text{N}_2\text{O}_2] - k_2[\text{N}_2\text{O}_2][\text{H}_2]$

The steady state approximation states that the net rate of formation of an intermediate must equal 0

\begin{align*}
0 &= k_1[\text{NO}]^2 - k_1'[\text{N}_2\text{O}_2] - k_2[\text{N}_2\text{O}_2][\text{H}_2] \\
[\text{N}_2\text{O}_2] &= k_1[\text{NO}]^2(k_1' + k_2[\text{H}_2])^{-1}
\end{align*}

Rate of formation of $\text{N}_2\text{O} = k_2 k_1[\text{H}_2][\text{NO}]^2(k_1' + k_2[\text{H}_2])^{-1}$
8) (10 pts) What is the binding energy per nucleon of $^{19}_9$F in J? The atomic mass of $^{19}_9$F is 18.9984 u.

$$9^1\text{H} + 10^1\text{n} \rightarrow 19^9\text{F}$$

Change mass of neutron into atomic mass units
$$1.67495 \times 10^{-27} \text{ kg (1 u / 1.6605} \times 10^{-27} \text{ kg)} = 1.0087 \text{ u}$$

$$\Delta m = m(19^9\text{F}) - (9 \cdot m(1^1\text{H}) + 10 \cdot m(1^0\text{n}))$$
$$= 18.99894 - (9 \cdot 1.0078 \text{ u} + 10 \cdot 1.0087 \text{ u})$$
$$= -0.15826 \text{ u}$$

$$\Delta m = -0.15826 \text{ u} \times (1.6605 \times 10^{-27} \text{ kg / 1 u}) = -2.6279 \times 10^{-28} \text{ kg}$$

$$E_{\text{bind}} = |\Delta m| \cdot c^2 = |-2.6279 \times 10^{-28} \text{ kg} | \times (3 \times 10^8 \text{ m/s})^2$$
$$= 2.36512 \times 10^{-11} \text{ J}$$

$$E_{\text{bind}} \text{ per nucleon} = 2.36512 \times 10^{-11} \text{ J} / 19 \text{ nucleons} = 1.24 \times 10^{-12} \text{ J/nucleon}$$

(6 pts) Calculate the energy change when one $^{235}_{92}$U nucleus undergoes the fission reaction

$$^{235}_{92}\text{U} + 1^1\text{n} \rightarrow 142_{56}\text{Ba} + 92_{36}\text{Kr} + 2^1\text{n}.$$  

The masses needed are $^{235}_{92}$U, 235.04 u; $^{142}_{56}$Ba, 141.92 u; $^{92}_{36}$Kr, 91.92; and $^1\text{n}$, 1.0087 u.

$$\Delta m = m(142_{56}\text{Ba}) + m(92_{36}\text{Kr}) + 2 \cdot m(1^0\text{n}) - m(235_{92}\text{U}) - m(1^1\text{n})$$
$$= 141.92 \text{ u} + 91.92 \text{ u} + 2(1.0087 \text{ u}) - 235.04 \text{ u} - 1.0087 \text{ u} = -0.1913 \text{ u}$$

$$\Delta m = -0.1913 \text{ u} \times (1.6605 \times 10^{-27} \text{ kg / 1 u}) = -3.1765 \times 10^{-28} \text{ kg}$$

$$E = |\Delta m| \cdot c^2 = 3.1765 \times 10^{-28} \text{ kg} \times (3 \times 10^8 \text{ m/s})^2 = -2.86 \times 10^{-11} \text{ J}$$
9) (5 pts) Write the shorthand notation for \( \text{Cu}^{2+} (aq) + \text{H}_2(g) \rightarrow 2\text{H}^+ (aq) + \text{Cu}^+ (aq) \).

\[
\text{Pt(s)|H}_2(g)|\text{H}^+(aq)||\text{Cu}^{2+}(aq),\text{Cu}^+(aq)|\text{Pt(s)}
\]

(2 pts) In the equation \( \text{Cu}^{2+}(aq) + \text{H}_2(g) \rightarrow 2\text{H}^+(aq) + \text{Cu}^+(aq) \) which species is oxidized?

\( \text{H}_2(g) \)

(3 pts) Which species is the strongest reducing agent?

\[
\begin{align*}
\text{Hg}_2^{2+}(aq) + 2\text{e}^- &\rightarrow 2\text{Hg}(l) & E^0 &= 0.79 \text{ V} \\
\text{In}^{2+}(aq) + \text{e}^- &\rightarrow \text{In}^+(aq) & E^0 &= -0.40 \text{ V} \\
\text{Al}^{3+}(aq) + 3\text{e}^- &\rightarrow \text{Al}(s) & E^0 &= -1.66 \text{ V}
\end{align*}
\]

\( \text{Al}(s) \)